Adaptive Wavelet Transform Based Rake Receiver for Ultra-Wideband Systems

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Abstract

This paper proposes a dual-tree complex wavelet transform (DTCWT) based adaptive rake receiver for Ultra-Wideband (UWB) systems. Advantage of using dual tree complex wavelet transform is that instead of capturing the signal energy in different multipath components at different delays, it captures them at different frequency components. LMS equalizer used in the receiver structure reduces the ISI. This adaptive scheme does not require all the parameters of the multipath components, but a short training period is only required to adjust the tap weights. The performance of the proposed receiver is evaluated and compared with existing conventional adaptive rake receiver and adaptive continuous wavelet transform rake receiver. All possible rake combinations such as ARAKE, SRAKE and PRAKE are considered, and it is found that the performance of the proposed system has shown a significant SNR improvement of 5-6 dB over conventional adaptive rake receiver.

Key words

UWB system, Rake receiver, Wavelet transform, DTCWT.

1. Introduction

The interest for low cost, fast, wireless connections for short range (<10 m) communication
is significantly expanding every day. The UWB system is a promising technology that gives a high information rate which makes it appropriate to be utilized as a part of many fields. The UWB transmission enables it to be utilized with systems and in many fields like PAN (Personal Area Network), WLAN (Wireless Local Area Network) and multimedia transmission frameworks and in the biomedical and military fields [1], [2]. A UWB system depends on the transmission of a train of ultra-short pulses over a wide bandwidth. As indicated by the FCC (Federal Communication Committee) regulations, the UWB frameworks are permitted to transmit over the frequency band of 3.1 to 10.6 GHz. The vast data transfer capacity secured by UWB frameworks, builds its possibility of interfering with other narrowband and wideband frameworks utilizing the low Gigahertz frequency bands. Therefore, the FCC regulations limit the UWB transmission. Where, the UWB frameworks can transmit just utilizing low power. The achievable data rates and transmission range of the system is limited by these strict regulations on the UWB system in addition to the channel effect which is extremely frequency selective [2], [3]. Since UWB transmits data utilizing ultra-short pulses in nanosecond, the UWB channel is enhanced with resolvable multipath components (i.e. it has a dense multipath condition). Thus, the received waveform is made up of many scaled and delayed replicas of transmitted signal.

Performance of the UWB system is enhanced by using a rake receiver that introduces multipath diversity to capture the most of the energy of the multipath components. A large number of rake fingers are required to transfer most of the transmission energy spread over the multipath components (correlator’s template waveforms are the delayed versions of the transmitted pulse). That is also the large range of channel parameters are need to estimated [2],[3].

A large number of research papers were presented on the Rake receiver which also includes the study of the performance of the partial, chip, or symbol delays spacing Rake with channel estimator [4]. Its execution was additionally studied with two combining strategies the MRC and SLC (Square Law Combiner) in [5]. Likewise a Selective Rake (SRake) receiver which tracks the strongest L multipath components is proposed in [6] with its execution exhibited. The Rake receiver is additionally examined with a MISO space–time coding utilizing MRC Rake receiver in [7] and [8], to make utilization of multipath diversity in addition to spatial diversity and thus improve the channel capacity. In [1] a smart UWB framework depending upon the utilization of analog STC scheme I (STC-I) with a GA Rake receiver was proposed that adaptively chooses the fingers delays to catch multipath components with maximum gain. A great enhancement in SNR for a single user scheme was showed by the smart UWB system. Its execution is additionally considered in combatting interference from other UWB frameworks utilizing Time Reversal (TR)
pre-coding method [9]. To accomplish an information rate of not less than 110Mbps for each user in UWB communication, the required symbol time should not exceed 10ns. As per [10], there is rms delay spread of 15ms for a channel model used for a range of 4-10 meter in Non-Line-of-sight environment. This spread shows that there is a significant inter-symbol interference (ISI) in fast UWB communication frameworks. The rake receiver just combines the energy of multipath components but does not prevent ISI. In [11], a rake- MMSE-equalizer structure was proposed. By far most of distributed outcomes on UWB ignored this reality as most execution investigations utilize a rake receiver under the presumption that channel delay spreads are a great deal not as much as the symbol time [12,13]. The wavelet transform (WT) has been widely utilized in the wireless communication field exclusively in UWB communication [14]. The WT was presented in [15] as new modulation scheme WSK (Wavelet Shift Keying) which is considered as a speculation of "Wavelet based orthogonal frequency division multiplexing (OFDM)". Likewise the OFDM scheme qualities are upgraded by utilizing orthogonal wavelet division multiplexing (OWDM) in a Rayleigh fading channel as represented in [16]. Then again the OFDM framework is considered with discrete wavelet transform (DWT) and discrete multi-wavelet transform (DMWT) to reduce the level of interference and increase the spectral efficiency in [17]. It is appeared in [18] that DMWT–OFDM proposes much lower bit error rate (BER), increases the signal to noise ratio (SNR), and therefore can be utilized as an alternative to the ordinary OFDM. Complex wavelet pulses enabling PSK Modulation for UWB impulse radio communications was presented in [19]. Continuous wavelet transform based rake receiver is designed and implemented in [20] for an UWB systems with high data rate. In [21] estimation of TOA for an OFDM-UWB based system is investigated with the help of wavelet packet transform. In [22] the performance for UWB communication systems using different optimal model techniques in a RAKE receiver is investigated.

In this paper, we present a novel dual tree complex wavelet transform (DTCWT) based adaptive rake receiver. This paper is organized as follows: Section 2 is focused on the UWB transmit model, UWB channel model, and the rake receiver in brief. Section 3 explains about the adaptive equalization technique, section 4 deals with the proposed rake receiver and section 5 gives the simulation results analysis. Section 6 concludes the paper.

2. System Model

This section, presents the system model used in this paper for an UWB systems for peer-to-peer communication. In the UWB communications binary symbols $S= \pm 1$ are transmitted over a train of ultra-short pulses. The binary symbol is pulse shaped by monocycle pulse (Gaussian
pulse 2nd derivative). Then the symbols are modulated by Pulse Amplitude Modulation (PAM) modulation and transmitted repeatedly over $N_f$ frames each of time duration $T_f$ ($T = N_f T_f$, where $T_f$ is the symbol duration). The pulse repetition, distribute the symbol energy over multiple frames of pulses to satisfy the FCC power regulations [14]. The pulse waveform $w(t)$ has typical duration $T_w$ between 0.2–2ns, resulting in transmission over an ultra-wide bandwidth. The transmitted waveform for the binary symbol $S$ is given by

$$ S(t) = s \sqrt{\frac{E}{N_f}} \sum_{n_f=0}^{N_f-1} w(t - n_f T_f) $$

(1)

where, $E$ is the symbol energy, and pulse shape $w(t)$ is of unit energy. The multipath channel can be expressed in terms of multipath delays and gains as given below.

$$ h(t) = \sum_{m=0}^{M-1} \alpha(m) \delta(t - \tau(m)) $$

(2)

where $h(t)$ is the impulse response of the UWB channel, $\alpha(m)$ and $\tau(m)$ are gain and delay. Impulse response of the UWB channel model in frequency domain is given as

$$ H(\omega) = \int_{-\infty}^{\infty} h(t) e^{-j\omega t} dt $$

(3)

where $H(\omega)$ is the Fourier transform of $h(t)$, $\omega$ is the angular frequency.

Note that, $\tau(m) > \tau(m-1)$, and $T_m = \tau(M-1)$ is the maximum delay spread of the dense multipath channel.

In the traditional RAKE structure, there are $L$ delayed pulse-matched filters and combiners. Because here the resolution of the multi-path profile is $1/W$, a sample alternative way to implement the traditional RAKE structure is considered. It just requires only one pulse-matched filter and sampling its output at $W$, the process is now a pure digital signal processing after all. Here assuming that system is perfectly synchronized, the pulse energy is 1 and no inter-pulse interference exists. Then this digital signal can be expressed in the form:
\[ r(t) = \sum_{n=1}^{L} \alpha_n s(t - \tau_n) + n(t) \]

(4)

where \( s(t) \) is the transmitted symbol, \( L \) is number of paths, \( n(t) \) is the additive white Gaussian noise, \( \tau_n \) is the delay of \( n^{th} \) path and \( \alpha_n \) is the gain of \( n^{th} \) path.

According to the UWB channel model from IEEE P802.15 [15], there are about 60 delayed paths which capture 85% total energy in the 4-10 meter range and non line of sight. In this paper Rake receiver is performance is evaluated by considering all the paths (ARAKE), N-selected paths (SRAKE) and first arriving multipath components (PRAKE). To implement a RAKE receiver, the arrival time, amplitude and phase of the fingers need to be estimated, a pilot signal approach is used in this investigation. \( N_p \) pilot bits are to be transmitted at the beginning of every data packet for channel estimation purpose. This results in a computational delay. In order to maximize the signal-to-noise ratio (SNR), MRC is used to collect the multipath diversity in two levels: The first level is to combine the fingers output of the Rake receiver for each frame. The second one is to combine the frames corresponding to the same symbol and finally to reduce the ISI LMS equalizer is used. Over all system block diagram is shown in Fig.1

![Fig.1. System Model](image)

3. Adaptive LMS Equalizer

In most communication systems that utilize equalizers, the channel attributes are ambiguous and, by and large, the channel reaction is time-variant. In such a case, the equalizers ought to be intended to be customizable to the channel reaction and, for time-variation channels, to be adaptable to the time variations in the channel reaction. From interpretation of the MSE criterion
linear equalization, an ideal tap weight coefficient \( \hat{I}_k \) can be obtained by solving a set of linear equations. This coefficient can be recursively acquired by the technique for steepest descent. This strategy is the fundamental of the LMS adaptive equalization. The recursive algorithm using in the equalizer can be operated by the time index \( k \) and the result can be equivalently expressed in the form of three basic relations as follows:

\[
\hat{I}_k = V^T(k) \hat{C}(k)
\]

(5)

\[
e(k) = I_k - \hat{I}_k
\]

(6)

\[
\hat{C}(k+1) = \hat{C}(k) + \mu V^T(k) e(k)
\]

(7)

Equations above define the estimation error \( e(k) \), computation of which is based on the current estimation of the equalizer coefficient vector \( \hat{C}(k) \). The iterative procedure begins with an appropriate initial guess on \( \hat{C}(0) \) and step size \( \mu \) and \( V \) is the received symbol. This algorithm is the complex form of the adaptive LMS algorithm. To acquire the estimation error \( e(k) \), the receiver must know about the transmitted data succession \( I_k \). Such learning can be made accessible amid a short training period in which a signal with a known data grouping is transmitted to the receiver. This training is used for initial adjusting of the equalizer tap weights. In practice, the training sequence is often selected to be a periodic pseudorandom sequence, such as a maximum length shift register sequence. After the training period, a practical scheme for continuous adjustment of the equalizer tap weights may be used. One scheme is a known pseudorandom-probe sequence is inserted in the information-bearing signal either additively or by interleaving in time. The tap weights are adjusted by comparing the received probe symbols with the known transmitted probe symbols. The convergence properties of the LMS algorithm are governed by a step-size parameter \( \mu \). The necessary condition that has to be satisfied for the convergence of the LMS algorithm is:
\[ 0 < \mu < \frac{2}{\lambda_{\text{max}}} \]  

(8)

where \( \lambda_{\text{max}} \) is the largest eigenvalue of the \((2K+1) \times (2K+1)\) correlation matrix. A significant feature of the LMS algorithm is its simplicity. Moreover, it does not require measurements of the pertinent correlation functions, nor does it require matrix inversion. Indeed, it is the simplicity of the LMS algorithm that has made it the standard against which the other linear adaptive equalization algorithms are benchmarked.

4. Proposed Rake Receiver

Figure 2 below shows the details of proposed rake receiver. First the dual tree complex wavelet transform (DTCWT) of each multipath component of received signal is taken and is correlated with the template signal or reference signal, which is a dual tree complex wavelet transformed of transmitted pulse.

![Fig.2. Proposed DTCWT Based Adaptive Rake Receiver Architecture.](image)

DTCWT consists of two levels. If it is used at level-1 the complexity gets reduced, but the performance of the system will be poor. Hence at level-2, the DTCWT is used in both the cases to improve the performance of the system. Maximum ratio combiner is used to combine all the fingers output. After the MRC combiner inverse dual tree complex wavelet transform is applied to convert back to time domain and decision logic and a LMS equalizer are used. The LMS equalizer updates the channel coefficients. Based on these channel coefficients rake parameters are recomputed and updated.
4.1 Dual Tree Complex Wavelet Transform

The discrete wavelet transform (DWT) is an implementation of the wavelet transform using a discrete set of the wavelet scales and translations obeying some defined rules. In other words, this transform decomposes the signal into mutually orthogonal set of wavelets, which is the main difference from the continuous wavelet transform (CWT), or its implementation for the discrete time series sometimes called discrete-time continuous wavelet transform. The wavelet can be constructed from a scaling function which describes its scaling properties. The restriction that the scaling functions must be orthogonal to its discrete translations implies some mathematical conditions on them which are mentioned everywhere, e.g. the dilation equation

\[ \varphi(x) = \sum_{k=\infty}^{\infty} a_k \varphi(Sx-k) \]

(9)

where \( \varphi(x) \) is the wavelet function and \( a_k \) is the gain and \( S \) is a scaling factor (usually chosen as 2). Moreover, the area between the function must be normalized and scaling function must be orthogonal to its integer translations. \( \Phi(x) \) is the wavelet function and \( a_k \) is the gain. There are several types of implementation of the DWT algorithm. The oldest and most known one is the Mallat (pyramidal) algorithm. In this algorithm two filters – smoothing and non-smoothing one – are constructed from the wavelet coefficients and those filters are recurrently used to obtain data for all the scales. If the total number of data \( D = 2^N \) is used and the signal length is \( L \), first \( D/2 \) data at scale \( L/2^{N-1} \) are computed, then \( (D/2)/2 \) data at scale \( L/2^{N-2} \), … up to finally obtaining 2 data at scale \( L/2 \). The result of this algorithm is an array of the same length as the input one, where the data are usually sorted from the largest scales to the smallest ones. The DTCWT is a relatively recent enhancement to the DWT, with important additional properties: it is nearly shift invariant and directionally selective in two and higher dimensions. The Dual tree complex wavelet transform comprises of two parallel DWT filter banks. The filter coefficients of these filter banks are designed in such way that, they minimize the aliasing effects due to down-sampling. Figure below shows the design of complex dual tree. For a given N point signal the dual tree complex transform gives 2N DWT Coefficients, as transform is two times expensive. To gain the maximum advantage of dual tree, filter coefficients of tree ‘a’ and tree ‘b’ DWTs shouldn’t be equal. So the filter coefficients are designed in such a way that tree ‘a’ DWT signal acts like a real part of the complex transform whereas the tree ‘b’ DWT signal acts like an imaginary component. Select of the filters in this way will result in a nearly shift invariant output, which is
major disadvantage in classical DWT. Dual tree uses the filter of order 10. The structure is shown in Fig.3

![Fig.3. Dual Tree Architecture.](image)

**5. Simulation Results**

Simulation results and the performance analysis of the proposed system over the existing systems are presented here. In this paper, the simulated system parameters were assumed to be 1000 bits. We can get accurate results by considering more number of random bits. As the number of bits increases simulation requires much time. 2\textsuperscript{nd} order derivative of Gaussian pulse of width 0.5ns is used as transmit pulse. The frame duration is assumed to be 20ns and the sampling interval is 0.05ns, therefore number of pulses per frame is 10. We have considered 1024 such frames and among, it is assumed that 128 frames are used for the system training purpose.

Based on the parameters and characteristics the UWB channel is classified in to four different types of channels denoted as CM1 to CM4. The CM1 and CM2 are based on measurements for LOS and Non-LOS environments over the distance of 0-4m, respectively. CM3 is based on measurements for Non-LOS environment over the distance of 4-10m. The CM4 is more realistic, as it supports extreme multipath conditions and Non-LOS environment. Hence Channel with NLOS of 4-10 mts (CM4) is considered for the simulation purpose. Fig. 4 below shows the performance of the rake receiver that considers all the 63 delayed paths which capture 85\% of total energy in the 4-10 meter range and non-line of sight. It is observed that the proposed adaptive receiver has shown an improved performance compared to conventional rake receiver. The DTCWT adaptive Rake receiver has shown 4dB improvement in SNR compared with conventional adaptive Rake receiver and 1dB improvement with adaptive CWT rake receiver. In this process ARAKE, SRAKE and PRAKEs are considered to evaluate the performance. In conventional Rake receiver the multipath delays are estimated in the time domain. The wavelet transform technique is not considered.
Fig.4. ARAKE: The BER Performance Adaptive Conventional ARAKE, Adaptive CWT - ARAKE and Adaptive DTCWT - ARAKE

Figures 5, 6 and 7 show the simulation results of a rake receiver which considers the first $L$ multipath components (PRAKE). In this case the performance of the proposed rake is significantly very high. It is found that the DTCWT adaptive Rake receiver has shown 5dB improvement and adaptive CWT rake receiver has shown 4dB improvement in SNR compared with conventional adaptive Rake receiver when first 8 multipath components are processed.

Fig.5. PRAKE: The BER Performance Ofl Adaptive Conventional PRAKE, Adaptive DTCWT PRAKE and Adaptive CWT PRAKE with $L=2$
Fig. 6. PRAKE: The BER Performance of Adaptive Conventional PRAKE, Adaptive CWT PRAKE and Adaptive DTCWT PRAKE with L=4

Fig. 7. PRAKE: The BER performance of Adaptive Conventional PRAKE, Adaptive CWT PRAKE and Adaptive DTCWT PRAKE with L=8
Fig. 8. SRAKE: The BER Performance of Adaptive Conventional SRAKE, Adaptive CWT SRAKE and Adaptive DTCWT SRAKE with L=2

Fig. 8, 9 and 10 show the performance of L-selective rake receiver (SRAKE), where L is number of rake fingers which takes values 2, 4, 8. The detailed simulation results clearly demonstrate that in fig.8, the DTCWT adaptive Rake receiver and CWT adaptive rake receiver has shown 5dB improvement in SNR compared with conventional adaptive Rake receiver, in fig.9, the DTCWT adaptive Rake receiver and CWT adaptive rake receiver has shown 5dB improvement in SNR compared with conventional adaptive Rake receiver and in fig.10 the DTCWT adaptive Rake receiver has shown 6dB improvement and adaptive CWT rake receiver has shown 5dB improvement in SNR compared with conventional adaptive Rake receiver.
Fig. 9. SRAKE: The BER Performance of Adaptive Conventional SRAKE, Adaptive CWT SRAKE and Adaptive DTCWT SRAKE with L=4

Fig. 10. SRAKE: The BER Performance of Adaptive Conventional SRAKE, Adaptive CWT SRAKE and Adaptive DTCWT SRAKE with L=8

**Conclusion**

An adaptive dual tree complex wavelet transform (DTCWT) rake receiver is designed and implemented for enhanced performance for UWB systems. The receiver structure uses a DTCWT, maximum ratio combiner (MRC) and a least mean square (LMS) equalizer. As the channel considered being blind, a training based channel estimation and LMS equalizer is
implemented and studied. Advantage of using dual tree complex wavelet transform is that instead of capturing the signal energy in different multipath components at different delays, it captures them at different frequency components. The proposed scheme does not require all the parameters of the multipath components, but a short training period is only required to adjust the tap weights. The performance of the proposed adaptive DTCWT rake receiver is evaluated and compared with existing conventional adaptive rake receiver and adaptive continuous wavelet transform rake receiver. It is found that the performance of the proposed system has shown a significant improvement in average SNR 5-6 dB over the conventional adaptive rake receiver.

References